



Uniwersytet
Wrocławski

X-ray Photoelectron Spectroscopy as a tool for control superlattice heterostructures quality and surface bilayer formation

Leszek Markowski

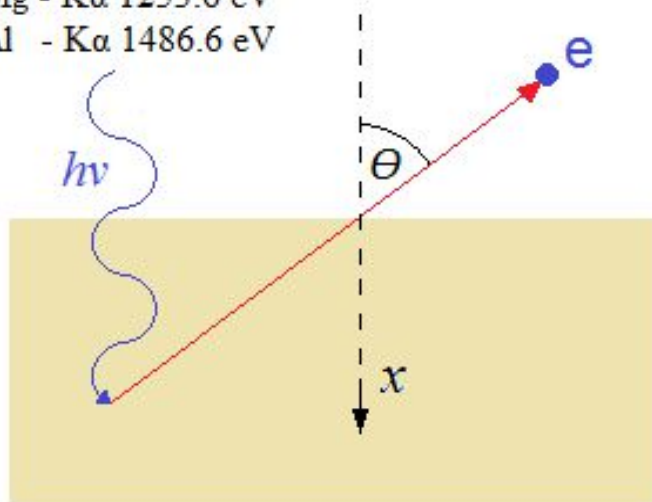
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Topics and motivation

- XPS as a tool for quantitative surface analysis
- How to control graphene formation by means of XPS
- Superlattice or heterostructure quality determination
- XPS application for quantitative analysis of graphene formation on superlattice substrate (e.g. on SiC, GaN)
- Thickness determination of an adlayer deposited on superlattice substrate

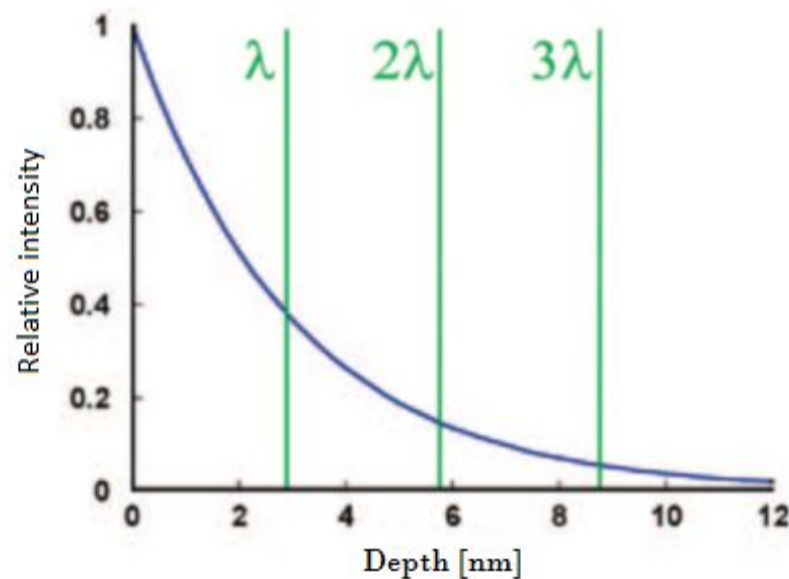
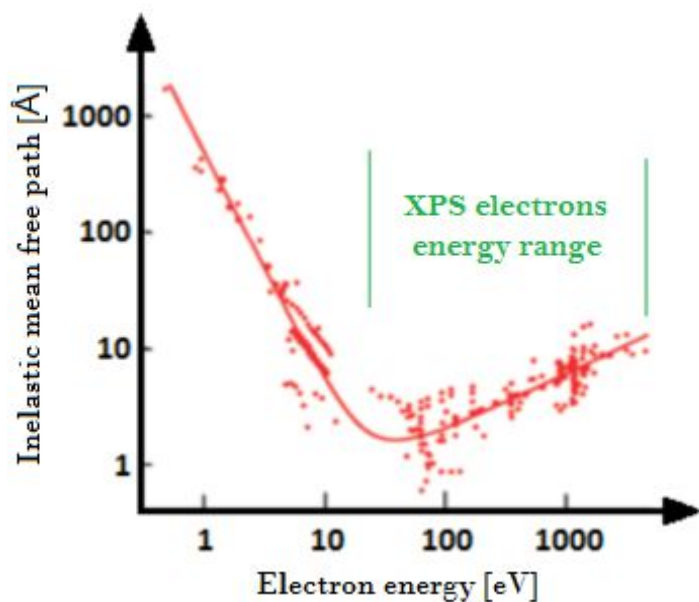
XPS and Beer-Lamberta Law

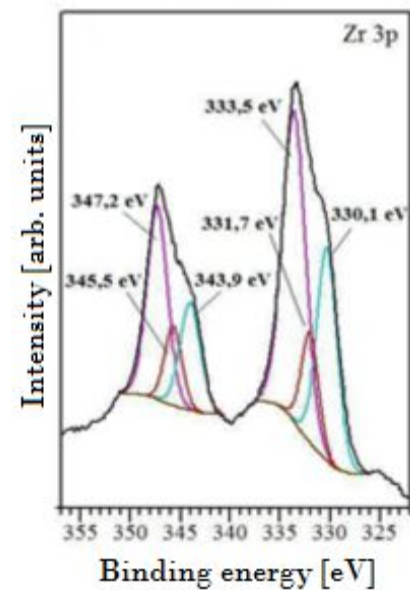
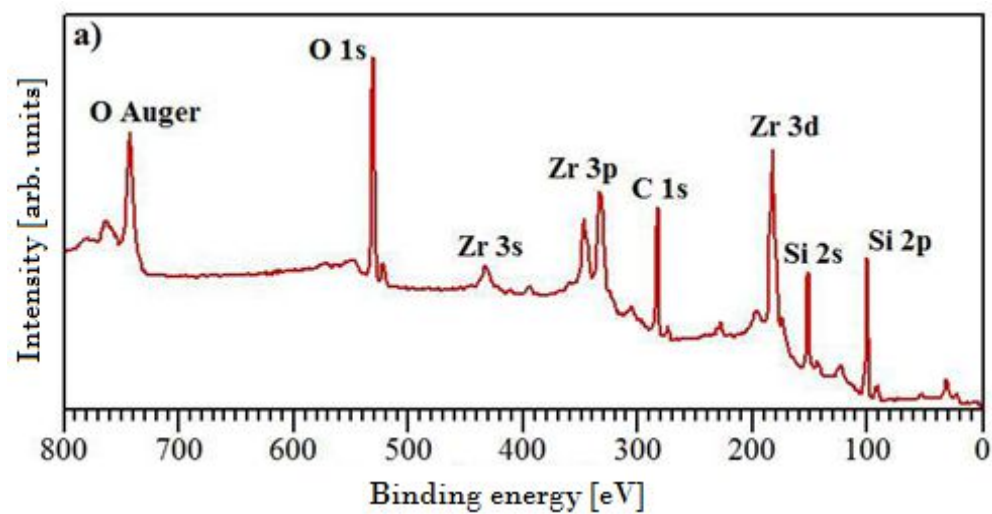
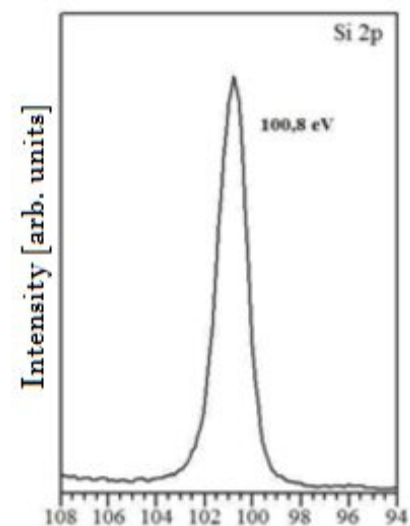
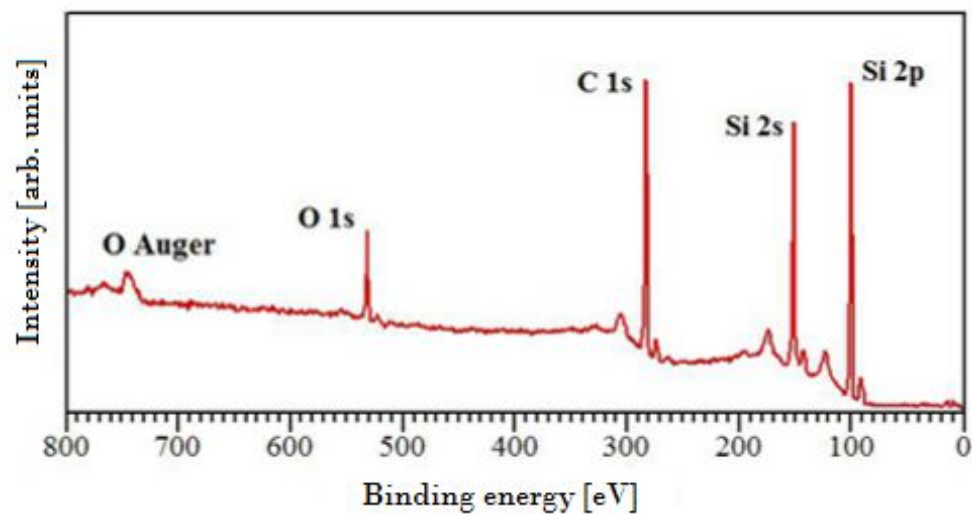
Mg - K α 1253.6 eV
Al - K α 1486.6 eV



Beer-Lambert Law

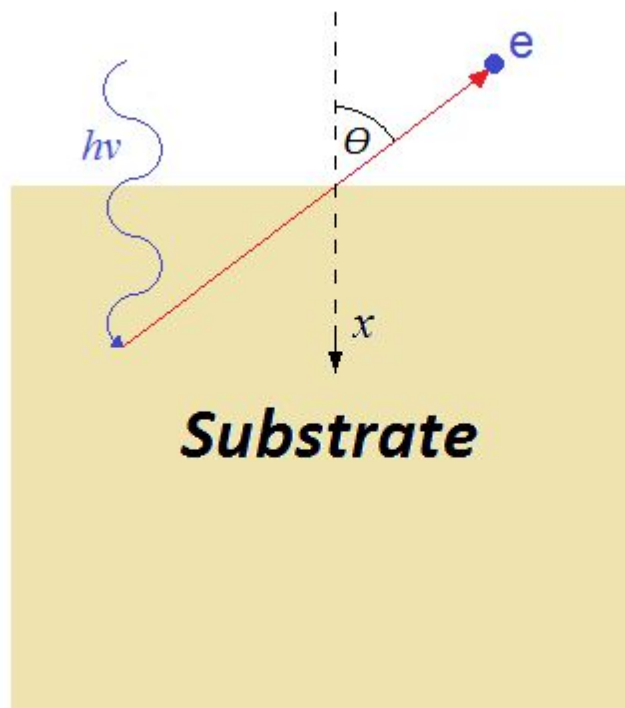
$$I(x) = I_0 \exp\left(-\frac{x}{\lambda \cos \theta}\right)$$





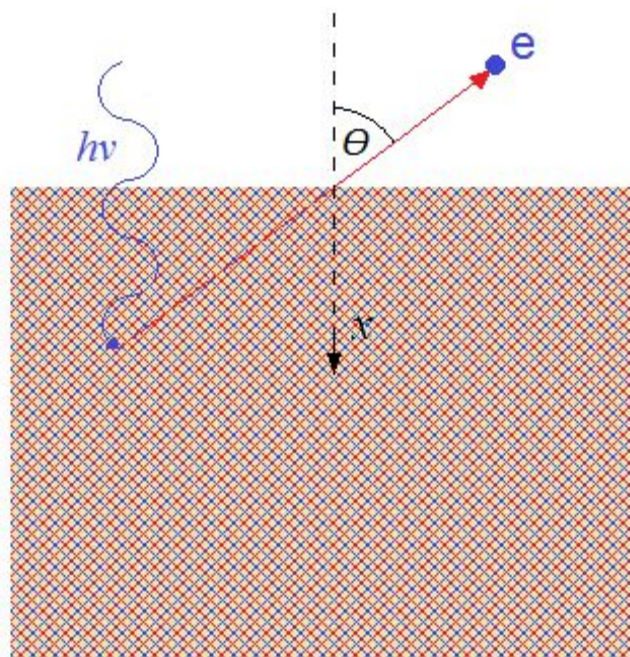
K. Idczak, Doctoral thesis, University of Wrocław 2014

XPS signal from the solid (one element only)



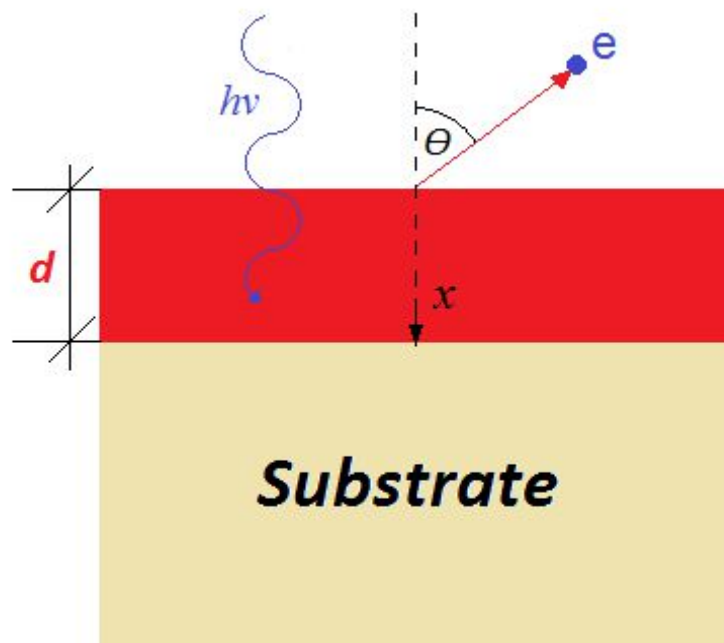
$$I_s(E_i) = k \int_0^{\infty} dI_s(E_i) = k \int_0^{\infty} n_s \sigma_s(E_i) \exp\left(-\frac{x}{\lambda_s(E_i) \cos \theta}\right) dx = k n_s \sigma_s(E_i) \lambda_s(E_i) \cos \theta$$

Atomic concentration in the solid (uniform composition)



$$n_i = \frac{\frac{I_i}{\sigma_i \lambda_i}}{\sum_{w=1}^{w=N} \frac{I_w}{\sigma_w \lambda_w}}$$

XPS signal for monoatomic adlayer deposited on a monoatomic substrate



$$\frac{I_s(E_i)}{I_{s0}(E_i)} = \exp\left(-\frac{d}{\lambda_a(E_i) \cos \theta}\right)$$

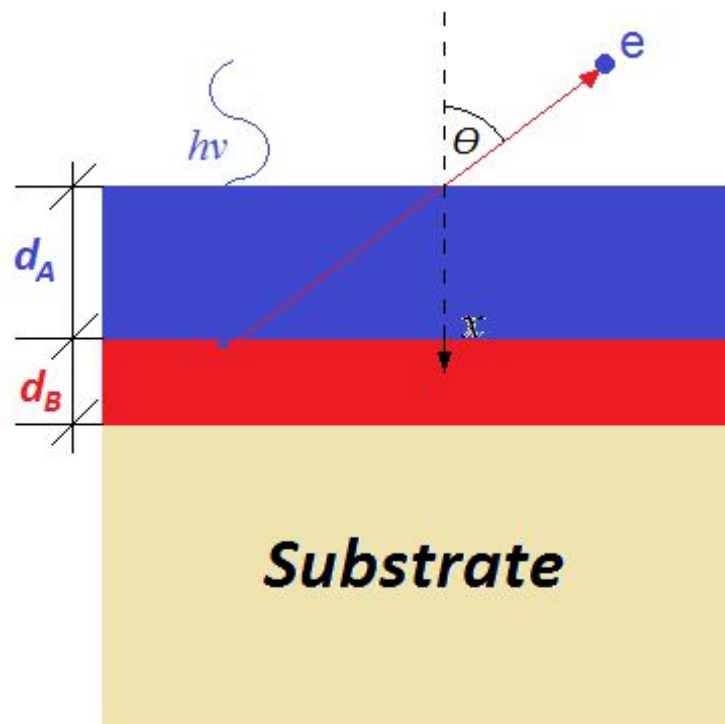
$$d = -\lambda_a(E_i) \cos \theta \ln \left[\frac{I_s(E_i)}{I_{s0}(E_i)} \right]$$

$$I_a(E_j) = k \int_0^d dI_a(E_j) = k \int_0^d n_a \sigma_a(E_j) \lambda_a(E_j) \exp\left(-\frac{x}{\lambda_a(E_j) \cos \theta}\right) dx = k n_a \sigma_a(E_j) \lambda_a(E_j) \left[1 - \exp\left(-\frac{d}{\lambda_a(E_j) \cos \theta}\right) \right]$$

$$\frac{I_a(E_j)}{I_s(E_i)} = \frac{n_a \sigma_a(E_j) \lambda_a(E_j)}{n_s \sigma_s(E_i) \lambda_s(E_i)} \left[\exp\left(-\frac{d}{\lambda_a(E_i) \cos \theta}\right) - \exp\left(\frac{d}{\cos \theta} \left(\frac{1}{\lambda_a(E_i)} - \frac{1}{\lambda_a(E_j)} \right) \right) \right]$$

$$d = \lambda_a(E_i) \cos \theta \ln \left[1 + \frac{I_a(E_j) n_s \sigma_s(E_i) \lambda_s(E_i)}{I_s(E_i) n_a \sigma_a(E_j) \lambda_a(E_j)} \right]$$

XPS signal for two monoatomic adlayers deposited on monoatomic substrate

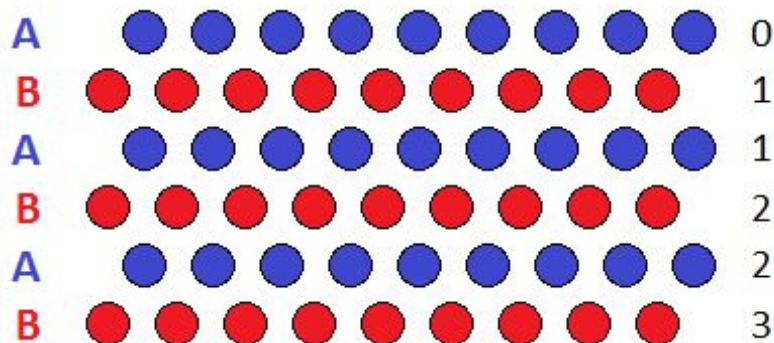


$$I_A(E_j) = kn_A \sigma_A(E_j) \lambda_A(E_j) \cos \theta \exp \left[1 - \left(-\frac{d_A}{\lambda_A(E_j) \cos \theta} \right) \right]$$

$$I_B(E_l) = kn_B \sigma_B(E_l) \lambda_A(E_l) \cos \theta \exp \left[1 - \left(-\frac{d_B}{\lambda_B(E_l) \cos \theta} \right) \right] * \exp \left(-\frac{d_A}{\lambda_A(E_l) \cos \theta} \right)$$

$$I_s(E_i) = kn_s \sigma_s(E_i) \lambda_s(E_i) \cos \theta \exp \left(-\frac{d_A}{\lambda_A(E_i) \cos \theta} \right) * \exp \left(-\frac{d_B}{\lambda_B(E_i) \cos \theta} \right)$$

XPS signal from crystal with two elements basis (e.g. SiC, GaN)



$$I_{A,0} = kn_A \sigma_A(E_{i,A})$$

$$I_{B,1} = kn_B \sigma_B(E_{i,B}) \exp(-n_A \delta_{B,A}(E_{i,B}) \cos \theta)$$

$$\delta_{B,B}(E_{i,B}) = \frac{1}{n_{B,bulk} \lambda_B(E_{i,B})}$$

$$I_{A,1} = kn_A \sigma_A(E_{i,A}) \exp(-n_B \delta_{A,B}(E_{i,A}) \cos \theta) \cdot \exp(-n_A \delta_{A,A}(E_{i,A}) \cos \theta)$$

$$I_{B,2} = I_{B,1} \exp(-n_A \delta_{B,A}(E_{i,B}) \cos \theta) \cdot \exp(-n_B \delta_{B,B}(E_{i,B}) \cos \theta)$$

$$I_{A,2} = I_{A,1} \exp(-n_B \delta_{A,B}(E_{i,A}) \cos \theta) \cdot \exp(-n_A \delta_{A,A}(E_{i,A}) \cos \theta)$$

$$I_{A,n} = I_{A,n-1} \exp(-n_B \delta_{A,B}(E_{i,A}) \cos \theta) \cdot \exp(-n_A \delta_{A,A}(E_{i,A}) \cos \theta)$$

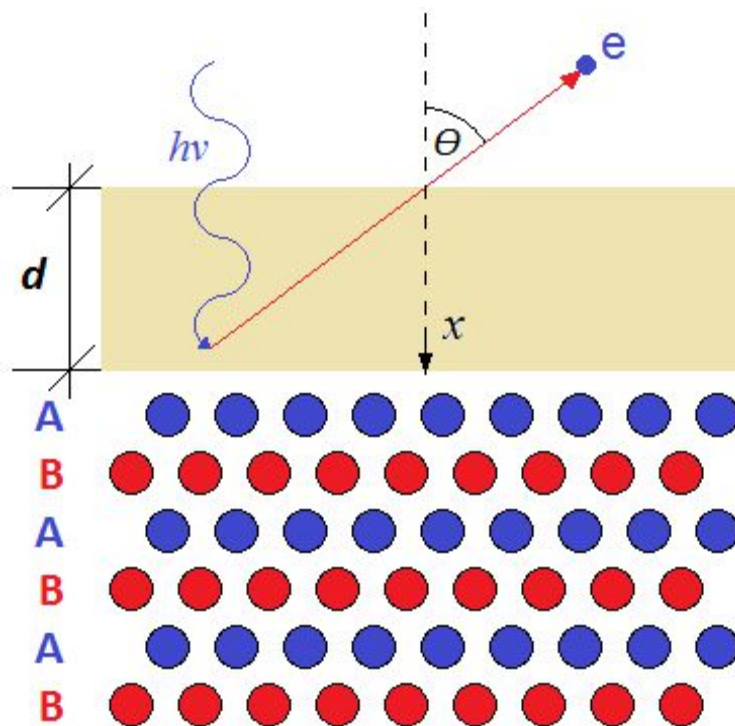
$$I_{B,n} = I_{B,n-1} \exp(-n_A \delta_{B,A}(E_{i,B}) \cos \theta) \cdot \exp(-n_B \delta_{B,B}(E_{i,B}) \cos \theta)$$

$$I_A = \sum_{n=0}^{\infty} I_{A,n} = \frac{I_{A,0}}{1 - \exp(-n_B \delta_{A,B}(E_{i,A}) \cos \theta) \cdot \exp(-n_A \delta_{A,A}(E_{i,A}) \cos \theta)}$$

$$I_B = \sum_{n=1}^{\infty} I_{B,n} = \frac{I_{B,1}}{1 - \exp(-n_A \delta_{B,A}(E_{i,B}) \cos \theta) \cdot \exp(-n_B \delta_{B,B}(E_{i,B}) \cos \theta)}$$

$$\sum_{n=1}^{\infty} aq^{n-1} = \frac{a}{1-q}$$

XPS signal for monoatomic adlayer deposited on two-elements crystal



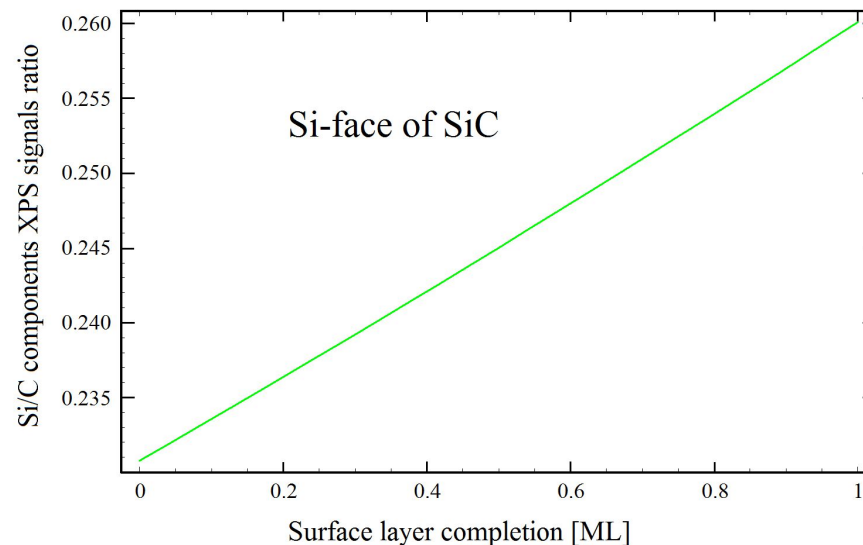
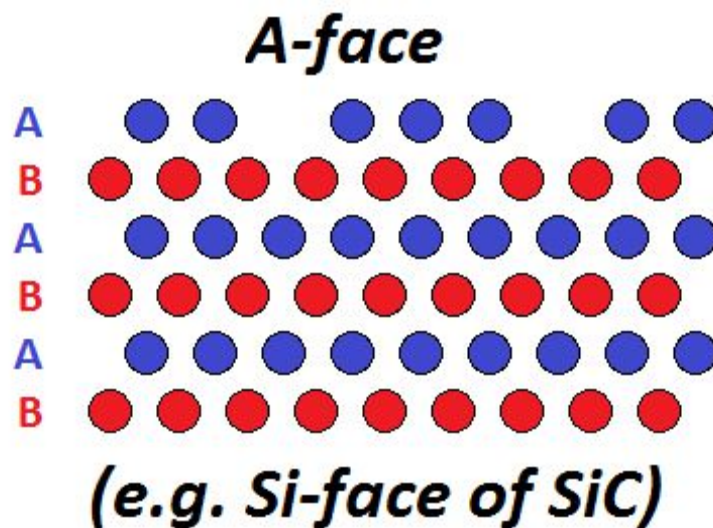
$$I_a(E_j) = kn_a \sigma_a(E_j) \lambda_a(E_j) \left[1 - \exp\left(-\frac{d}{\lambda_a(E_j) \cos \theta}\right) \right]$$

$$I_{Aa} = I_A \cos \theta \exp\left(-\frac{d}{\lambda_a(E_{i,A}) \cos \theta}\right)$$

$$I_{Ba} = I_B \cos \theta \exp\left(-\frac{d}{\lambda_a(E_{i,B}) \cos \theta}\right)$$

$$\frac{I_a(E_j)}{I_{Aa}(E_{i,A})} = \frac{n_a \sigma_a(E_j) \lambda_a(E_j)}{n_A \sigma_A(E_{i,A})} \left[1 - \exp\left(-\frac{d}{\lambda_a(E_j) \cos \theta}\right) \right] \left[1 - \exp(-n_B \delta_{A,B}(E_{i,A}) \cos \theta) \cdot \exp(-n_A \delta_{A,A}(E_{i,A}) \cos \theta) \right]$$

XPS signal from two-elements crystal during surface layer decomposition



$$I_{A,0} = Pkn_A\sigma_A(E_{i,A})$$

$$I_{B,1} = kn_B\sigma_B(E_{i,B})\exp(-Pn_A\delta_{B,A}(E_{i,B})\cos\theta)$$

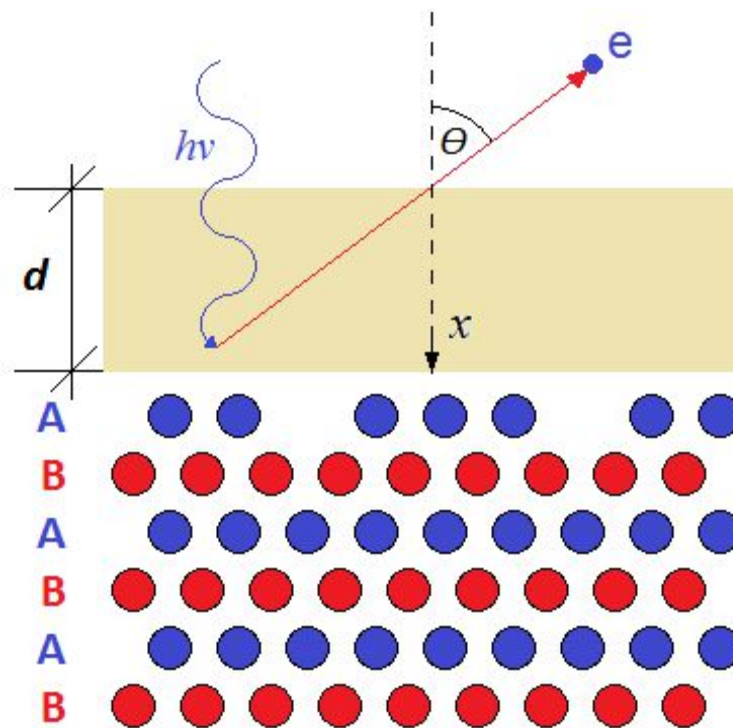
P - first layer filling coefficient

$$I_{A,1} = kn_A\sigma_A(E_{i,A})\exp(-n_B\delta_{A,B}(E_{i,A})\cos\theta)\cdot\exp(-Pn_A\delta_{A,A}(E_{i,A})\cos\theta)$$

$$I_A = \sum_{n=1}^{\infty} I_{A,n} = \frac{I_{A,1}}{1 - \exp(-n_B\delta_{A,B}(E_{i,A})\cos\theta)\cdot\exp(-n_A\delta_{A,A}(E_{i,A})\cos\theta)} + I_{A,0}$$

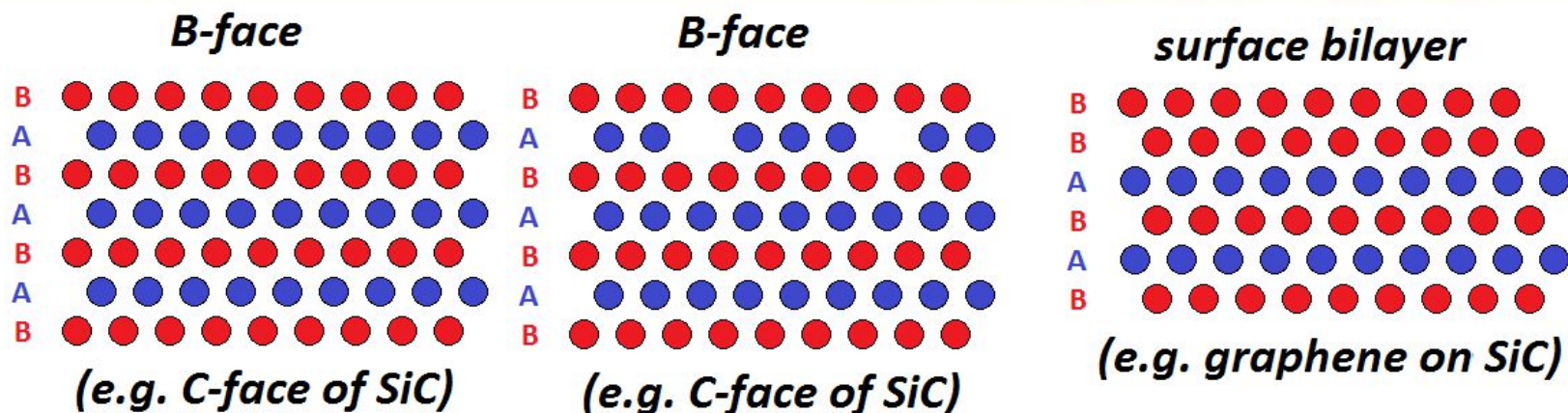
$$I_B = \sum_{n=1}^{\infty} I_{B,n} = \frac{I_{B,1}}{1 - \exp(-n_A\delta_{B,A}(E_{i,A})\cos\theta)\cdot\exp(-n_B\delta_{B,B}(E_{i,B})\cos\theta)}$$

XPS signal for monoatomic adlayer deposited on two-elements crystal with incomplete surface layer



$$\frac{I_a(E_j)}{I_{Ba}(E_{i,B})} = \frac{n_a \sigma_a(E_j) \lambda_a}{n_B \sigma_B(E_{i,B})} \left[1 - \exp\left(-\frac{d}{\lambda_a(E_j) \cos \theta}\right) \right] \\
 [1 - \exp(-n_A \delta_{B,A}(E_{i,A}) \cos \theta) \cdot \exp(-n_B \delta_{B,B}(E_{i,B}) \cos \theta)] \exp(P n_A \delta_{B,A}(E_{i,B}) \cos \theta)$$

Surface bilayer formation on two-elements crystal (e.g. graphene on SiC)



$$I_{B,0} = kn_B \sigma_B(E_{i,B})$$

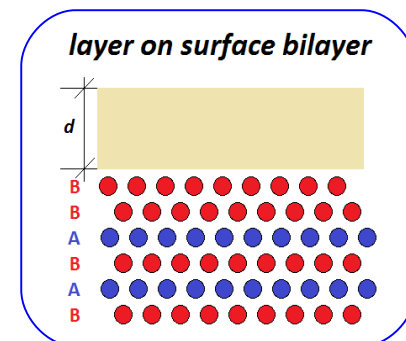
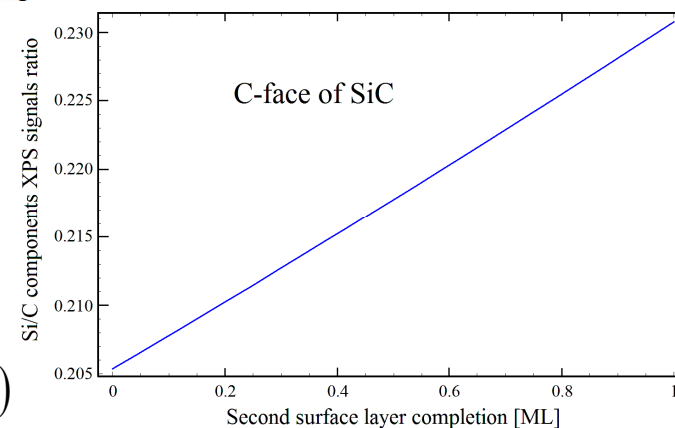
$$I_{A,1} = Pkn_A \sigma_A(E_{i,A}) \exp(-n_B \delta_{A,B}(E_{i,A}) \cos \theta)$$

$$I_{B,1} = kn_B \sigma_B(E_{i,B}) \exp(-Pn_A \delta_{B,A}(E_{i,B})) \cdot \exp(-n_B \delta_{B,B}(E_{i,B}))$$

$$I_{A,2} = \frac{I_{A,1}}{P} \exp(-n_B \delta_{A,B}(E_{i,A}) \cos \theta) \cdot \exp(-Pn_A \delta_{A,A}(E_{i,A}) \cos \theta)$$

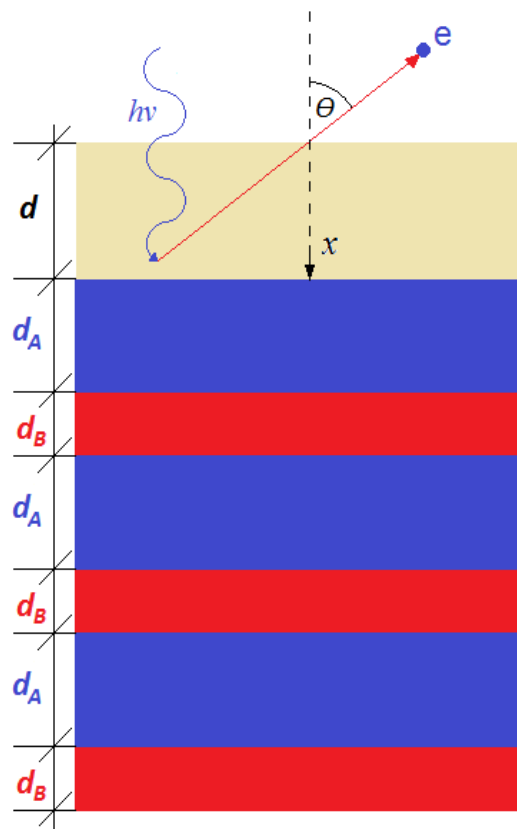
$$I_B = \sum_{n=1}^{\infty} I_{B,n} = \frac{I_{B,1}}{1 - \exp(-n_A \delta_{B,A}(E_{i,B}) \cos \theta) \cdot \exp(-n_B \delta_{B,B}(E_{i,B}) \cos \theta)} + I_{B,0}$$

$$I_A = \sum_{n=2}^{\infty} I_{A,n} = \frac{I_{A,2}}{1 - \exp(-n_B \delta_{A,B}(E_{i,B}) \cos \theta) \cdot \exp(-n_A \delta_{A,A}(E_{i,A}) \cos \theta)} + I_{A,1}$$



Thickness determination of an adlayer deposited on superlattice substrate

adlayer on superlattice



$$\frac{I_a(E_j)}{I_{Aa}(E_{i,A})} = \frac{n_a \sigma_a(E_j) \lambda_a}{n_{A,bulk} \sigma_A(E_{i,A}) \lambda_A(E_{i,A})} \left[\frac{1 - \exp\left(-\frac{d}{\lambda_a(E_j) \cos \theta}\right)}{1 - \exp\left(-\frac{d_A}{\lambda_A(E_{i,A}) \cos \theta}\right)} \right] \left[1 - \exp\left(-\frac{d_B}{\lambda_B(E_{i,A}) \cos \theta}\right) \exp\left(-\frac{d_A}{\lambda_A(E_{i,A}) \cos \theta}\right) \right]$$



Thank you for your attention!